

## NOTES: Section 9.6 – Solving Quadratic Equations by the Quadratic Formula

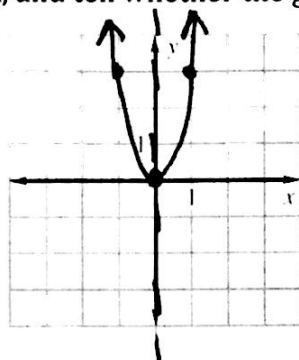
Goals: #1 - I can use the quadratic formula to solve a quadratic equation.

*Homework: Section 9.6 Worksheet*



**Warm Up:** Graph the function by completing the table. Identify the graph's axis of symmetry (AOS), vertex, and tell whether the graph opens up or down.

1.  $y = 3x^2 + 0x + 0$



AOS:  $x = 0$

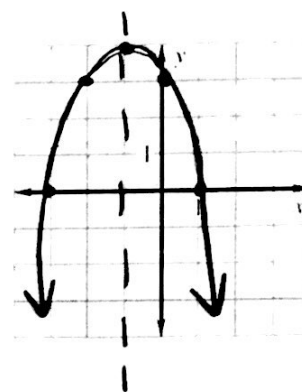
vertex:  $(0, 0)$

y-int:  $(0, 0)$

opens: up

solution/s: 0

2.  $y = -x^2 - 2x + 3$



AOS:  $x = -1$

vertex:  $(-1, 4)$

y-int:  $(0, 3)$

opens: down

solution/s: -3, 1

x	-2	-1	0	1	2
y	12	3	0	3	12

$$x = \frac{-b}{2a} = \frac{-(0)}{2(3)} = 0$$

x	-3	-2	-1	0	1
y	0	3	4	3	0

$$x = \frac{-b}{2a} = \frac{-(-2)}{2(-1)} = \frac{2}{-2} = -1$$

**Review:**

A quadratic equation in standard form:  $y = ax^2 + bx + c$

To put a quadratic equation in standard form, we set the equation equal to 0.

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Let's practice: Write the equation in standard form. Identify the values of  $a$ ,  $b$ , and  $c$ .

1.  $3x^2 = 3x + 6$   
 $-3x \quad -3x$

$3x^2 - 3x = 6$   
 $-b \quad -b$   
 $3x^2 - 3x - 6 = 0$

$a = \underline{3}$

$b = \underline{-3}$

$c = \underline{-6}$

2.  $-2x^2 = -8$   
 $+8 \quad +8$

$-2x^2 + 8 = 0$

$a = \underline{-2}$

$b = \underline{0}$

$c = \underline{8}$

3.  $-x^2 + 5x = 6$   
 $-b \quad -b$

$-x^2 + 5x - 6 = 0$

$a = \underline{-1}$

$b = \underline{5}$

$c = \underline{-6}$

4.  $-24x + 45 = -3x^2$   
 $+3x^2 \quad +3x^2$

$3x^2 - 24x + 45 = 0$

$a = \underline{3}$

$b = \underline{-24}$

$c = \underline{45}$

Notes:

We can solve ANY quadratic equations by using the quadratic formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Step 1: Set the quadratic equation equal to 0.

Step 2: Plug and chug!

Example #1: Use the quadratic formula to solve the equation. Round the solutions to the nearest tenth, if necessary.

1.  $x^2 + 9x + 14 = 0$

$a = \underline{1}$

$b = \underline{9}$

$c = \underline{14}$

①  $x^2 + 9x + 14 = 0 \checkmark$

②  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$x = \frac{-(9) \pm \sqrt{(9)^2 - 4(1)(14)}}{2(1)}$

$x = \frac{-9 \pm \sqrt{81 - 56}}{2}$

$x = \frac{-9 \pm \sqrt{25}}{2}$

$x = \frac{-9 \pm 5}{2}$

$x = \frac{-9+5}{2} = \frac{-4}{2} = -2$

$x = \frac{-9-5}{2} = \frac{-14}{2} = -7$

$x = -2$
$x = -7$

2.  $2x^2 - 3x = 8$

$a = \underline{2}$

$b = \underline{-3}$

$c = \underline{-8}$

①  $2x^2 - 3x = 8$   
 $-8 \quad -8$

$2x^2 - 3x - 8 = 0 \checkmark$

②  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4(2)(-8)}}{2(2)}$

$x = \frac{3 \pm \sqrt{9 + 64}}{2}$

$x = \frac{3 \pm \sqrt{73}}{2}$
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You practice: Use the quadratic formula to solve the equation. Round the solutions to the nearest tenth, if necessary.

3.  $7x^2 - 1 = -2x$

$a = \underline{7}$

$b = \underline{2}$

$c = \underline{-1}$

①  $7x^2 - 1 = -2x$   
 $\quad \quad \quad +2x \quad +2x$

$7x^2 + 2x - 1 = 0 \checkmark$

②  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$x = \frac{-(2) \pm \sqrt{(2)^2 - 4(7)(-1)}}{2(7)}$

$x = \frac{-2 \pm \sqrt{4 + 28}}{14}$

$x = \frac{-2 \pm \sqrt{32}}{14} < \frac{\sqrt{16}}{\sqrt{2}}$

$x = \frac{-2 \pm 4\sqrt{2}}{14}$

$x = \frac{-1 \pm 2\sqrt{2}}{7}$

You practice: Write down the quadratic 5 times!

1.  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

2.  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

3.  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

4.  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

5.  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$