

Name: \_\_\_\_\_ Hour: \_\_\_\_\_ Date: \_\_\_\_\_

## NOTES: Section 7.5 – Apply Properties of Logarithms

Goals: #1 - I can use properties of a logarithm to evaluate logarithms.

#2 - I can use properties of a logarithm to expand and condense logarithms.

#3 - I can use the change of base formula to evaluate logarithms.



*Homework: Lesson 7.5 Worksheet*

### Warm Up:

1. Rewrite the equation in its alternate form.

a.  $\log 10,000 = 4$

b.  $e^7 = x - 3$

2. Evaluate the logarithm without a calculator.

a.  $\log_6 216$

b.  $\log_{16} \frac{1}{4}$

c.  $\log_{1/4} 16$

3. Find the inverse of the function.

a.  $y = \log(x - 2)$

b.  $y = (0.4)^x$

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**Exploration #1:** Work with a partner and answer the following questions.

1. Let  $x = \log_b m$  and  $y = \log_b n$

a. Rewrite these logarithmic equations in exponential form:

$$x = \log_b m \rightarrow$$

$$y = \log_b n \rightarrow$$

b. Now multiply  $mn$ :

$$mn =$$

c. Rewrite this exponential equation in logarithmic form:

$$mn = b^{x+y} \rightarrow$$

2. Let  $x = \log_b m$  and  $y = \log_b n$

a. Rewrite these logarithmic equations in exponential form:

$$x = \log_b m \rightarrow$$

$$y = \log_b n \rightarrow$$

b. Now divide  $\frac{m}{n}$ :

$$\frac{m}{n} =$$

c. Rewrite this exponential equation in logarithmic form:

$$\frac{m}{n} = b^{x-y} \rightarrow$$

**Notes:**

\_\_\_\_\_:

<b>Product Property</b>	
<b>Quotient Property</b>	
<b>Power Property</b>	

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**Example #1:** Use  $\log_4 3 \approx 0.792$  and  $\log_4 7 \approx 1.404$  to evaluate the logarithm.

1.  $\log_4 \frac{3}{7}$

2.  $\log_4 21$

3.  $\log_4 49$

**Example #2:** Use the properties of logarithms to expand or condense the following expressions.

1. Expand  $\log_6 \frac{5x^3}{y}$

2. Condense  $\log 2 + 3 \log 3 - \log 9$

**You practice:** Use the properties of logarithms to expand or condense the following expressions.

1. Expand  $\log_3 \frac{7x^2}{y}$

2. Condense  $\ln 4 + 3 \ln 3 - \ln 12$

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**Notes:**

\_\_\_\_\_:

Since our calculators can only evaluate logarithms with base \_\_\_\_\_, we can use the change-of-base formula to evaluate \_\_\_\_\_ logarithm using a calculator.

**Example #3:** Use the change-of-base formula to evaluate the logarithm.

1.  $\log_3 8$

2.  $\log_6 11$

**Extra practice:**

1. Expand  $\log_7 \frac{3x^2}{5y^3}$

2. Condense  $5 \log_4 2 + 7 \log_4 x - 4 \log_4 y$