

NOTES: Section 11.5 Adding and Subtracting with Like Denominators.

Goals: #1 - I can add and subtract rational expressions with like denominators.

Homework: Section 11.5 Worksheet



Warm Up:

1. Find the product of the rational expression and simplify.

a. $\frac{4x}{3x^2} \cdot \frac{6x^3}{2x}$

$$\frac{2 \cdot 2 \cdot \cancel{x}}{3 \cdot \cancel{x} \cdot \cancel{x}} \cdot \frac{3 \cdot 2 \cdot \cancel{x} \cdot \cancel{x} \cdot \cancel{x}}{2 \cdot \cancel{x}}$$

$$\frac{\cancel{2} \cdot \cancel{2} \cdot \cancel{3} \cdot \cancel{2} \cdot \cancel{x} \cdot \cancel{x} \cdot \cancel{x}}{\cancel{3} \cdot \cancel{x} \cdot \cancel{x} \cdot \cancel{2} \cdot \cancel{x}}$$

4x

b. $\frac{x-1}{2x+2} \cdot \frac{4}{3x-3}$

$$\frac{x-1}{2(x+1)} \cdot \frac{2 \cdot 2}{3(x-1)}$$

$$\frac{\cancel{2} \cdot 2 \cdot \cancel{(x-1)}}{\cancel{2} \cdot 3 \cdot (x+1) \cdot \cancel{(x-1)}}$$

$\frac{2}{3(x+1)}$

2. Find the quotient of the rational expression and simplify.

a. $\frac{3(2x+1)}{2x-8} \div \frac{8x+4}{3(x-4)}$

$$\frac{3(2x+1)}{2(x-4)} \cdot \frac{3(x-4)}{4(2x+1)}$$

$$\frac{3 \cdot 3 \cdot \cancel{(2x+1)} \cdot \cancel{(x-4)}}{2 \cdot 4 \cdot \cancel{(x-4)} \cdot \cancel{(2x+1)}}$$

$\frac{9}{8}$

b. $\frac{5x^2+14x-3}{5x^2-x} \div (4x+12)$

$5 \cdot -3 = -15$
 $-14 = 15 + -1$

$$\frac{5x^2+15x-1x-3}{5x(x+3)-1(x+3)}$$

$$\frac{(x+3)(5x-1) \cdot \frac{1}{4(x+3)}}{(x+3)(5x-1)}$$

$$\frac{4 \cdot x \cdot \cancel{(5x-1)} \cdot \cancel{(x+3)}}{\cancel{(x+3)} \cdot \cancel{(5x-1)}}$$

$\frac{1}{4x}$

Exploration #1: Work with a partner and add the following fractions.

1. $\frac{3}{5} + \frac{1}{5}$

$\frac{4}{5}$

2. $\frac{2}{3} + \frac{2}{3}$

$\frac{4}{3}$

3. $\frac{1}{4} + \frac{3}{4}$

$\frac{4}{4}$

1

Name: _____ Hour: _____ Date: _____

Notes:

As with fractions, to add or subtract rational expressions with like denominators, combine their numerators and keep the common denominator.

Example #1: Add the rational expression and simplify.

1. $\frac{5}{2x} + \frac{x-5}{2x}$

$$\frac{5+x-5}{2x}$$

$$\frac{x}{2x}$$

$$\boxed{\frac{1}{2}}$$

$1 \cdot 1 = 1$
 $1 + 1 = 2$
 $x^2 + 1x + 1x + 1$
 $x(x+1) + 1(x+1)$
 $(x+1)(x+1)$

2. $\frac{2x}{x^2+2x+1} + \frac{2}{x^2+2x+1}$

$$\frac{2x+2}{x^2+2x+1}$$

$$\frac{2(x+1)}{(x+1)(x+1)}$$

$$\boxed{\frac{2}{x+1}}$$

You practice: Add the rational expression and simplify.

1. $\frac{x+2}{x} + \frac{3x-2}{x}$

$$\frac{x+2+3x-2}{x}$$

$$\frac{4x}{x}$$

$$\boxed{4}$$

$1 \cdot -5 = -5$
 $4 = 5 + -1$
 $a^2 + 5a - 1a - 5$
 $a(a+5) - 1(a+5)$
 $(a+5)(a-1)$

2. $\frac{a^2-2}{a^2-25} + \frac{4a-3}{a^2-25}$

$$\frac{a^2-2+4a-3}{a^2-25}$$

$$\frac{a^2+4a-5}{a^2-25}$$

$$\frac{(a+5)(a-1)}{(a+5)(a-5)}$$

$$\boxed{\frac{a-1}{a-5}}$$

Example #2: Subtract the rational expression and simplify.

$$1. \frac{x+2}{x^2+5} - \frac{3x+2}{x^2+5}$$

$$\frac{x+2 - (3x+2)}{x^2+5}$$

$$\frac{x+2-3x-2}{x^2+5}$$

$$\boxed{\frac{-2x}{x^2+5}}$$

$$3 \cdot -2 = -6$$

$$\quad \wedge$$

$$-3 + 2 = -1$$

$$\frac{3x^2 - 3x}{x^2+5} \Big| \frac{2x - 2}{x^2+5}$$

$$3x(x-1) + 2(x-1)$$

$$(3x+2)(x-1)$$

$$2. \frac{4x}{3x^2-x-2} - \frac{x-2}{3x^2-x-2}$$

$$\frac{4x - (x-2)}{3x^2-x-2}$$

$$\frac{4x - x + 2}{3x^2-x-2}$$

$$\frac{3x+2}{3x^2-x-2}$$

$$\frac{3x+2}{(3x+2)(x-1)}$$

$$\boxed{\frac{1}{x-1}}$$

You practice: Subtract the rational expression and simplify.

$$1. \frac{3x-4}{x-4} - \frac{2x}{x-4}$$

$$\frac{3x-4-2x}{x-4}$$

$$\frac{x-4}{x-4}$$

$$\boxed{1}$$

$$2 \cdot 5 = 10$$

$$\quad \wedge$$

$$-5 \quad -2$$

$$\frac{2x^2 - 5x}{x-4} \Big| \frac{-2x + 5}{x-4}$$

$$x(2x-5) - 1(2x-5)$$

$$(x-1)(2x-5)$$

$$2. \frac{1-x}{2x^2-7x+5} - \frac{3-3x}{2x^2-7x+5}$$

$$\frac{1-x - (3-3x)}{2x^2-7x+5}$$

$$\frac{1-x-3+3x}{2x^2-7x+5}$$

$$\frac{2x-2}{2x^2-7x+5}$$

$$\frac{2(x-1)}{(x-1)(2x-5)}$$

$$\boxed{\frac{2}{2x-5}}$$