

## NOTES: Section 5.7 – Apply the Fundamental Theorem of Algebra

Goals: #1 - I can identify the number of solutions or zeros in a polynomial.

#2 - I can find all the zeros (real, imaginary, and repeated) in a polynomial.

#3 - I can write a polynomial with given zeros.

#4 - I can determine the number and type of zeros of a polynomial given the degree and graph.

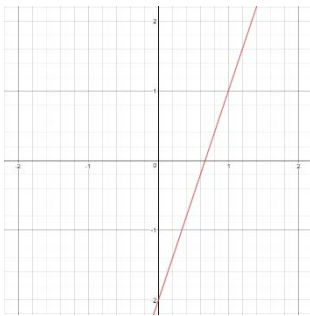


*Homework: Lesson 5.7 Worksheet*

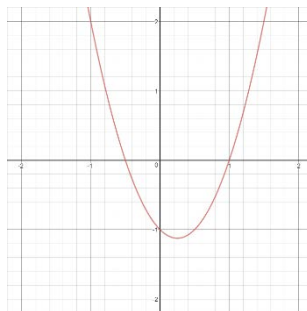
**Exploration #1:** Work with a partner and answer the following questions.

1. How many zeros are in the following graph?

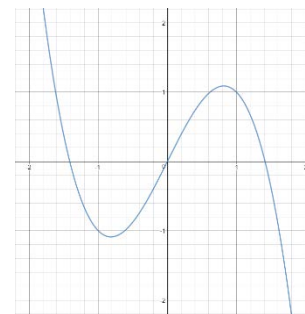
$$f(x) = 3x - 2$$



$$f(x) = 2x^2 - x - 1$$



$$f(x) = -x^3 + 2x$$



**Notes:**

- \_\_\_\_\_:
- If a \_\_\_\_\_  $f(x)$  has a \_\_\_\_\_, then the equation  $f(x) = 0$  has exactly \_\_\_\_\_, given each \_\_\_\_\_ counts as \_\_\_\_\_.

**Example #1:** Find the number of solutions or zeros of the following polynomial.

1.  $x^3 + 5x^2 + 4x + 20 = 0$

2.  $f(x) = x^4 - 8x^3 + 18x^2 - 27$

Name: \_\_\_\_\_ Hour: \_\_\_\_\_ Date: \_\_\_\_\_

**Example #2:** Find all zeros of the polynomial function.

1.  $f(x) = x^5 - 4x^4 + 4x^3 + 10x^2 - 13x - 14$

**You practice:** Find all zeros of the polynomial function.

1.  $f(x) = x^5 - 2x^4 + 8x^2 - 13x + 6$

Name: \_\_\_\_\_ Hour: \_\_\_\_\_ Date: \_\_\_\_\_

**Notes:**

- \_\_\_\_\_:
- If a \_\_\_\_\_  $f(x)$  has \_\_\_\_\_ as an imaginary zero, then \_\_\_\_\_ is also a \_\_\_\_\_ of  $f$ .
- If a \_\_\_\_\_  $f(x)$  has \_\_\_\_\_ as an imaginary zero, then \_\_\_\_\_ is also a \_\_\_\_\_ of  $f$ .

**Example #3:** Write a polynomial function  $f$  of least degree that has rational coefficients, a leading coefficient of 1, and 3 and  $2 + \sqrt{5}$  as zeros.

**You practice:** Write a polynomial function  $f$  of least degree that has rational coefficients, a leading coefficient of 1, and 2,  $2i$ , and  $4 - \sqrt{6}$  as zeros.